CSCE 235 Apr 7, 01

Quiz #4

Name: SSN: Row:

**Instructions:** Do *ONLY* **four** of the following questions. **Circle** the questions which you want to be graded and **cross out** those which you do **not** want to be graded.

**NOTE:** If you do not follow the instructions above, you may lose some points.

**Question 1:** (5 points) What is the degree sequence of  $\overline{C_n}$ ?

Solution: n-3, n-3, ..., n-3 (n of them).

**Question 2:** (5 points) When does  $\overline{C_n}$  have an Euler cycle?

Solution: When n is odd and  $n \geq 5$ .

**Question 3:** (5 points) Let G be a simple graph with a degree sequence  $k_1$ ,  $k_2$ ,  $k_3$ ,  $k_4$ ,  $k_5$ ,  $k_6$ ,  $k_7$ . What is the degree sequence of  $\overline{G}$ ?

Solution:  $6 - k_7$ ,  $6 - k_6$ ,  $6 - k_5$ ,  $6 - k_4$ ,  $6 - k_3$ ,  $6 - k_2$ ,  $6 - k_1$ .

**Question 4:** (5 points) Let G be a simple graph with a degree sequence  $k_1$ ,  $k_2$ ,  $k_3$ ,  $k_4$ ,  $k_5$ ,  $k_6$ ,  $k_7$ . How many edges does  $\overline{G}$  have?

Solution:  $21 - \frac{\sum_{i=1}^{7} k_i}{2}$ .

**Question 5:** (5 points) Let G be a simple graph with n vertices and k edges, how many edges does  $\overline{G}$  have?

Solution:  $\frac{n(n-1)}{2} - k$ .

**Question 6** (5 points) What is the degree sequence of  $K_n$ ?

Solution: n - 1, n - 1, ..., n - 1 (*n* of them).

**Question 7** (5 points) When does  $K_n$  have an Euler cycle?

Solution: When n is odd.

**Question 8** (5 points) How many edges does the n-cube have?

Solution:  $n \cdot 2^{n-1}$ .