

Name: ..... SSN: ..... Row: ....

**Question 1:** Let  $R$  be the relation on  $\mathbb{Z}$  defined by:

$$aRb \text{ iff } 3a + b \text{ is a multiple of } 4.$$

Prove that  $R$  is transitive and find  $R^{-1}$ . Also, find all of the equivalence classes.

**Question 2:** Define the following relation on  $R^2$ :

$$(a, b)R(c, d) \text{ iff } a^2 + b^2 = c^2 + d^2.$$

Find  $[(\alpha, \beta)]$ . What does  $[(\alpha, \beta)]$  represent in the Cartesian plane? Also, find  $R^{-1}$ .

**Question 3:** Let  $R$  be a relation on a set  $X$ . Prove or disprove:

1.  $R$  is symmetric.
2.  $R$  is transitive.
3.  $R$  is reflexive.